

## Psychrometric Formulae

**A. AIR MIXING EQUATIONS  
(Outdoor and Return Air)**

$$tm = \frac{(cfm_{oa} \times t_{oa}) + (cfm_{ra} \times h_{ra})}{cfm_{sa}}$$

$$hm = \frac{(cfm_{oa} \times h_{oa}) + (cfm_{ra} \times h_{ra})}{cfm_{sa}} \quad (2)$$

$$wm = \frac{(cfm_{oa} \times W_{oa}) + (cfm_{ra} \times h_{ra})}{cfm_{sa}} \quad (3)$$

**B. COOLING LOAD EQUATIONS**

$$ERSH = RSH + (BF)(OASH) + RSHS^* \quad (4)$$

$$ERLH = RLH + (BF)(OALH) + RLHS^* \quad (5)$$

$$ERTH = ERLH + ERSR \quad (6)$$

$$TSH = RSH + OASH + RSHS^* \quad (7)$$

$$TLH = RLH + OALH + RLHS^* \quad (8)$$

$$GTH = TSH + TLH + GTHS^* \quad (9)$$

$$RSH = 1.08 \times cfm_{sa} \times (t_{rm} - t_{sa}) \quad (10)$$

$$RLH = 0.68 \times cfm_{sa} \times (W_{rm} - W_{sa}) \quad (11)$$

$$RTH = 4.45 \times cfm_{sa} \times (h_{rm} - h_{sa}) \quad (12)$$

$$RTH = RSH + RLH \quad (13)$$

$$OASH = 1.08 \times Cfm_{oa} \times (toa - trm) \quad (14)$$

$$OALH = 0.68 \times cfm_{oa} \times (W_{oa} - W_{rm}) \quad (15)$$

$$OATH = 4.45 \times cfm_{oa} \times (hoa - h_{rm}) \quad (16)$$

$$OATH = OASH + OALH \quad (17)$$

$$(BF)(OATH) = (BF)(OASH) + (BF)(OALH) \quad (18)$$

$$ERSH = 1.08 \times Cfm_{da} \times (t_{rm} - t_{adp}) (1-BF) \quad (19)$$

$$ERLH = 0.68 \times Cfm_{da} \times (W_{rm} - W_{adp}) (1-BF) \quad (20)$$

$$ERTH = 4.45 \times Cfm_{da} \times (h_{rm} - h_{adp}) (1-BF) \quad (21)$$

$$TSH = 1.08 \times Cfm_{da} \times (t_{edp} - t_{adp})^{**} \quad (22)$$

$$TLH = 0.68 \times Cfm_{da} \times (W_{ea} - W_{la})^{**} \quad (23)$$

$$GTH = 4.45 \times Cfm_{da} \times (hea - h_{la})^{**} \quad (24)$$

**C. SENSIBLE HEAT FACTOR EQUATIONS**

$$RSHF = \frac{RSH}{RSH + RLH} = \frac{RSH}{RTH} \quad (25)$$

$$ESHF = \frac{ERSH}{RSH + ERLH} = \frac{ERSH}{RTRH} \quad (26)$$

$$GSHF = \frac{RSH}{TSH + TLH} = \frac{TSH}{GTH} \quad (26)$$

**D. BYPASS FACTOR EQUATIONS**

$$BF = \frac{t_{ldb} - t_{adp}}{t_{edp} - t_{adp}} = \frac{t_{edb} - t_{ldb}}{t_{edb} - t_{adp}} \quad (27)$$

$$BF = \frac{W_{la} - W_{adp}}{W_{ea} - W_{adp}} = \frac{W_{ea} - W_{la}}{W_{ea} - W_{adp}} \quad (29)$$

$$BF = \frac{h_{la} - h_{adp}}{h_{ea} - h_{adp}} = \frac{h_{ea} - h_{la}}{h_{ea} - h_{adp}} \quad (30)$$

**E. TEMPERATURE EQUATIONS AT APPARATUS**

$$t_{edb}^{**} = \frac{(cfm_{oa} \times t_{oa}) + (cfm_{ra} \times t_{ra})}{cfm_{sa} \#} \quad (31)$$

$$t_{ldb} = t_{adp} + BF(t_{edb} - t_{adp}) \quad (32)$$

$t_{edb}^{**}$  and  $t_{hwb}$  correspond to the calculated values of  $h_{ea}$  and  $h_{la}$  on the psychrometric chart.

$$h_{ea}^{**} = \frac{(cfm_{oa} \times h_{oa}) + (cfm_{ra} \times h_{ra})}{cfm_{sa} \#} \quad (33)$$

$$h_{ldb} = ht_{adp} + BF(h_{ea} - h_{adp}) \quad (34)$$

**F. TEMPERATURE EQUATIONS FOR SUPPLY AIR**

$$tsa = trm - \frac{RSH}{1.08 (cfm_{sa} \#)} \quad (35)$$

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G. AIR QUANTITY EQUATIONS

ERSH

$$cfm_{da} = 1.08 \times (1-BF) (t_{rm} - t_{adp}) \quad (36)$$

ERLH

$$cfm_{da} = \frac{0 \times (1-BF) (W_{rm} - W_{adp})}{4.45 \times (h_{rm} - h_{adp})} \quad (37)$$

ERTH

$$cfm_{da} = \frac{1.08 \times (1-BF) (t_{edp} - t_{ldp})}{4.45 \times (h_{rm} - h_{adp})} \quad (38)$$

TSH

$$cfm_{da} = \frac{1.08 \times (1-BF) (t_{edp} - t_{ldp})}{0.68 \times (W_{ea} - W_{ia})} \quad (39)$$

TLH

$$cfm_{da} \ddagger = \frac{0.68 \times (W_{ea} - W_{ia})}{4.45 \times (h_{ea} - h_{ia})} \quad (40)$$

GTH

$$cfm_{da} \ddagger = \frac{4.45 \times (h_{ea} - h_{ia})}{1.08 \times (t_{rm} - T_{sa})} \quad (41)$$

RSH

$$cfm_{sa} \ddagger = \frac{1.08 \times (t_{rm} - T_{sa})}{0.68 \times (W_{rm} - W_{sa})} \quad (42)$$

RLH

$$cfm_{sa} = \frac{0.68 \times (W_{rm} - W_{sa})}{4.45 \times (h_{rm} - h_{sa})} \quad (43)$$

RTH

$$cfm_{da} = \frac{4.45 \times (h_{rm} - h_{sa})}{cfm_{sa} - cfm_{da}} \quad (44)$$

$$cfm_{da} = cfm_{sa} - cfm_{da} \quad (45)$$

Note :  $cfm_{da}$  will be less than  $cfm_{sa}$  only when air is physically bypassed around the conditioning apparatus.

$$cfm_{sa} = cfm_{oa} - cfm_{ra} \quad (45)$$

$$1.08 = \frac{0.244 \times 60}{13.5}$$

Where 0.244 = Specific heat of moist air at 70 F db and 50% rh, Btu / (deg F) (lb dry air).

60 = min./hr  
13.5 = specific volume of moist air at 70 F db and 50% rh

$$0.68 = \frac{60}{13.5} \times \frac{107}{700}$$

Where 60 = min./hr  
13.5 = Specific volume of moist air at 70 F db and 50% rh

1076 = average heat removal required to condense one pound of water vapor from the room air

7000 = grains per pound

$$4.45 = \frac{60}{13.5}$$

Where 60 = min./hr  
13.5 = Specific volume of moist air at 70 F db and 50% rh

\* RSHS, RLHS and GTHS are supplementary loads due to duct heat gain, duct leakage loss, fan and pump horsepower gains, etc. To simplify the various examples, these supplementary loads have not been used in the calculations. However, in actual practice, these supplementary loads should be used where appropriate. Note :  $cfm_{da}$  will be less than  $cfm_{sa}$  only when air is physically bypassed around the conditioning apparatus.

‡ When no air is to be physically bypassed around the conditioning apparatus,  $cfm_{da} = cfm_{sa}$ .

\*\* When  $t_m$ ,  $W_m$  and  $h_m$  are equal to the entering conditions at the cooling apparatus, they may be substituted for  $t_{edp}$ ,  $W_{ea}$  and  $h_{ea}$  respectively.

## ABBREVIATIONS

Adp	Apparatus Dewpoint
BF	Bypass Factor
(BF) (OALH)	Bypassed Outdoor Air Latent Heat
(BF) (OASH)	Bypassed Outdoor Air Sensible Heat
But/hr	British Thermal Units per hour
Cfm	cubic feet per minute
db	Dry-Bulb Temperature
dp	Dewpoint
ERLH	Effective Room Latent Heat
ERSH	Effective Room Sensible Heat
ERTH	Effective Room Total Heat
ESHF	Effective Sensible Heat Factor
F	Fahrenheit degrees
fpm	feet per minute
gpm	gallons per minute
gr/lb	grains per pound
GSHF	Grand Sensible Heat Factor
GTHS	Grand Total Heat Supplement
OALH	Outdoor Air Latent Heat
OASH	Outdoor Air Sensible Heat
OATH	Outdoor Air Total Heat
rh	relative humidity
RLH	Room Latent Heat
RLHS	Room Latent Heat Supplement
RSH	Room Sensible Heat
RSHF	Room sensible heat supplement
RSHS	Room Latent Heat supplement
RTH	Room Total Heat
Sat Eff	saturation efficiency of spray
SHF	Sensible Heat Factor
TLH	Total Latent Heat
TSH	Total Sensible Heat
w b	wet bulb

## SYMBOLS

$cfm_{ba}$	Bypassed Air Quantity around Apparatus
$cfm_{da}$	Dehumidified Air Quantity
$cfm_{oa}$	Outdoor Air Quantity
$cfm_{ra}$	Return Air Quantity
$cfm_{sa}$	Supply Air Quantity
$h$	Specific Enthalpy
$h_{adp}$	Apparatus Dewpoint Enthalpy
$h_{es}$	Effective Surface Temperature Enthalpy
$h_{ea}$	Entering Air Enthalpy
$h_{ia}$	Leaving Air Enthalpy
$h_m$	Mixture of Outdoor and Return Air Enthalpy
$h_{oa}$	Outdoor Air Enthalpy
$h_{ra}$	Room Air Enthalpy
$h_{sa}$	Supply Air Enthalpy
$t$	Temperature
$t_{adp}$	Apparatus Dewpoint Temperature
$t_{edb}$	Entering Dry-Bulb Temperature
$t_{es}$	Effective Surface Temperature
$t_{ew}$	Entering Water Temperature
$t_{ewb}$	Entering Wet-Bulb Temperature
$t_{ldb}$	Leaving Dry-Bulb Temperature
$t_{lwb}$	Leaving Wet-Bulb Temperature
$t_m$	Mixture of Outdoor and Return Air Dry-Bulb Temperature
$t_{oa}$	Outdoor Air Dry-Bulb Temperature
$t_{im}$	Room Dry-Bulb Temperature
$t_{sa}$	Supply Air Dry-Bulb Temperature
$W$	Moisture Content or Specific Humidity
$W_{adp}$	Apparatus Dewpoint Moisture Content
$W_{ea}$	Entering Air Moisture Content
$W_{es}$	Effective Surface Temperature Moisture Content
$W_{ia}$	Leaving Air Moisture Content
$W_m$	Mixture of Outdoor and Return Dry Moisture Content
$W_{oa}$	Outdoor Air Moisture Content
$W_m$	Room Moisture Content
$W_{sa}$	Supply Air Moisture Content